

Lecture 2

Outline

2.3 Scientific Notation

2.4 Significant figures and Accuracy

3.1 Structure and Building Principles of Atoms

3.2 Element Symbols

3.3 Masses and the Mole

3.4 Introduction of the Periodic Table

Scientific Notation

Mole

The number of atoms in 12 g of carbon:

602,200,000,000,000,000,000

In science **6.022×10^{23}**

The mass of a single carbon atom in grams:

0.0000000000000000000000199

In science **1.99×10^{-23}**

$N \times 10^n$

n is a positive or negative integer

N is a number between 1 and 10

Scientific Notation and Significant Figures

568.762

← move decimal left

$n > 0$

$568.762 = 5.68762 \times 10^2$

0.00000772

→ move decimal right

$n < 0$

$0.00000772 = 7.72 \times 10^{-6}$

Uncertainty in Measurement

- Uncertainties always exist in measured quantities
- Measured quantities are generally reported in such a way that only the last digit is uncertain.
- All digits of a measured quantity, including the uncertain one, are called significant figures.

Sample Problem

Determining the Number of Significant Figures

PROBLEM: For each of the following quantities, underline the zeros that are significant figures (sf), and determine the number of significant figures in each quantity. For (d) to (f) express each in exponential notation first.

(a) 0.0030 L

(b) 0.1044 g

(c) 53.069 mL

(d) 0.00004715 m

(e) 57,600. s

(f) 0.0000007160 cm³

PLAN: Determine the number of sf by counting digits and paying attention to the placement of zeros.

SOLUTION:

(a) 0.0030 L 2sf

(b) 0.1044 g 4sf

(c) 53.069 mL 5sf

(d) 0.00004715 m

(e) 57,600. s

(f) 0.0000007160 cm³

(d) 4.715 $\times 10^{-5}$ m 4sf

(e) 5.7600 $\times 10^4$ s 5sf

(f) 7.160 $\times 10^{-7}$ cm³ 4sf

Rules for Significant Figures in Answers

- **For addition and subtraction.** The answer has the *same number of decimal places as there are in the measurement with the fewest decimal places.*

Example: adding two volumes:

$$\begin{array}{r} 83.5 \text{ mL} \\ + 23.28 \text{ mL} \\ \hline 106.78 \text{ mL} = 106.8 \text{ mL} \end{array}$$

Example: subtracting two volumes:

$$\begin{array}{r} 865.9 \text{ mL} \\ - 2.8121 \text{ mL} \\ \hline 863.0879 \text{ mL} = 863.1 \text{ mL} \end{array}$$

Rules for Significant Figures in Answers

- **For multiplication and division.** The number with the least certainty limits the certainty of the result. Therefore, *the answer contains the same number of significant figures as there are in the measurement with the fewest significant figures.*

Multiply the following numbers:

$$9.2 \text{ cm} \times 6.8 \text{ cm} \times 0.3744 \text{ cm} = 23.4225 \text{ cm}^3 = 23 \text{ cm}^3$$

Rules for Rounding Off Numbers

1. If the digit removed is *5 or more than 5*, the preceding number increases by 1. 5.379 rounds to 5.38 if three significant figures are retained and to 5.4 if two significant figures are retained.
2. If the digit removed is *less than 5*, the preceding number is unchanged. 0.2413 rounds to 0.241 if three significant figures are retained and to 0.24 if two significant figures are retained.
3. Be sure to carry two or more additional significant figures through a **multistep calculation** and round off only the *final* answer.

Sample Problem

Significant Figures and Rounding

PROBLEM: Perform the following calculations and round the answer to the correct number of significant figures.

$$(a) \frac{16.3521 \text{ cm}^2 - 1.448 \text{ cm}^2}{7.085 \text{ cm}} \qquad (b) \frac{4.80 \times 10^4 \text{ mg} \left(\frac{1 \text{ g}}{1000 \text{ mg}} \right)}{11.55 \text{ cm}^3}$$

PLAN: In (a) we subtract before we divide; for (b) we are using an exact number.

SOLUTION:

$$(a) \frac{16.3521 \text{ cm}^2 - 1.448 \text{ cm}^2}{7.085 \text{ cm}} = \frac{14.904 \text{ cm}^2}{7.085 \text{ cm}} = 2.104 \text{ cm}$$
$$(b) \frac{4.80 \times 10^4 \text{ mg} \left(\frac{1 \text{ g}}{1000 \text{ mg}} \right)}{11.55 \text{ cm}^3} = \frac{48.0 \text{ g}}{11.55 \text{ cm}^3} = 4.16 \text{ g/cm}^3$$

Precision and Accuracy Errors in Scientific Measurements

Precision -

Refers to *reproducibility* or how close the measurements are to each other.

Accuracy -

Refers to how close a measurement is to the real value.

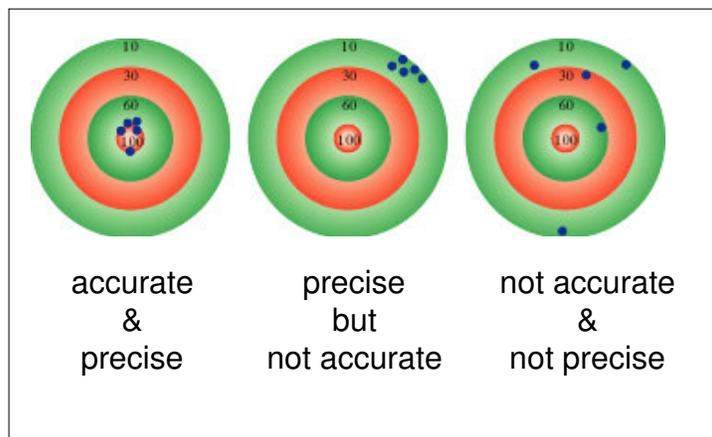
Systematic error -

Values that are either all higher or all lower than the actual value.

Random Error -

In the absence of systematic error, some values that are higher and some that are lower than the actual value.

Precision and Accuracy



Atoms

- Atoms **cannot** be sub-divided by **chemical reactions**: available energies are not high enough
- Atoms **can** be subdivided, modified or transferred into new atoms by **physical reactions** (nuclear reactions)
Reason: energies are sufficiently high
- Chemical properties of atoms are significantly determined by the elemental building units of atoms

Structure of Atoms:

Atom: built from **elementary particle**

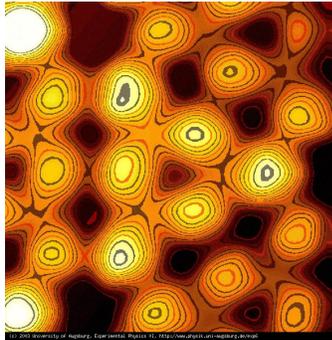
elementary particle

Material particles which cannot be divided into smaller particles, but they can react to give other elementary particles

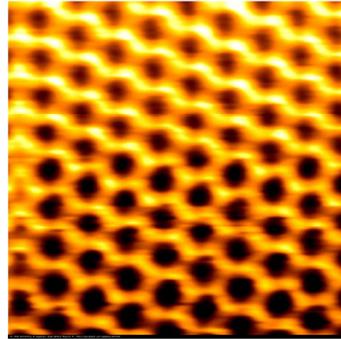
Protons, neutron, electrons (valid for nearly all atoms: exception the hydrogen atom)

Different atoms: Differ in the number and arrangement of elementary particles

Imaging Atoms



silicon



graphite

..... Atomic Force Microscopy or Scanning Tunnelling Microscopy

Building Principles of Atoms

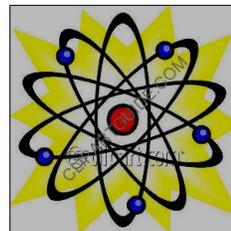
atom → elementary units

name (symbol)	mass (u)	charge (e)
Proton	1	+1
Neutron	1	-
Electron	0.0005	-1

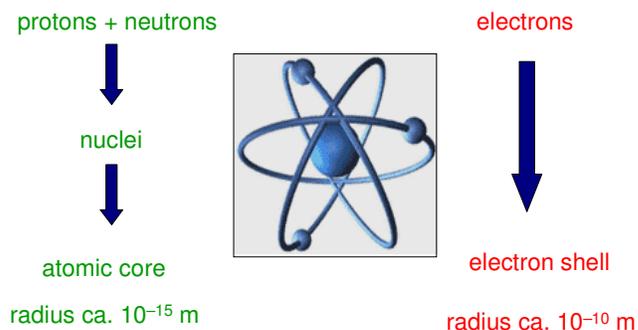
Atomic mass unit u: $1u = 1.6606 \cdot 10^{-27} \text{ kg}$

Elementary charge e: $1e = 1.6022 \cdot 10^{-19} \text{ C}$

smallest charge, observed in nature



Building Principles of Atoms



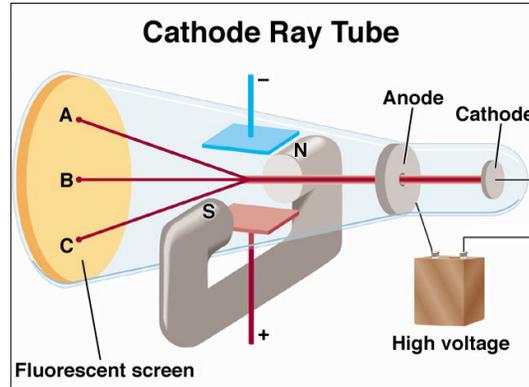
$$\text{Proton Number} + \text{Neutron Number} = \text{Mass Number}$$

..... Historical Aspects of these Discoveries.

Dalton's Atomic Theory (1805)

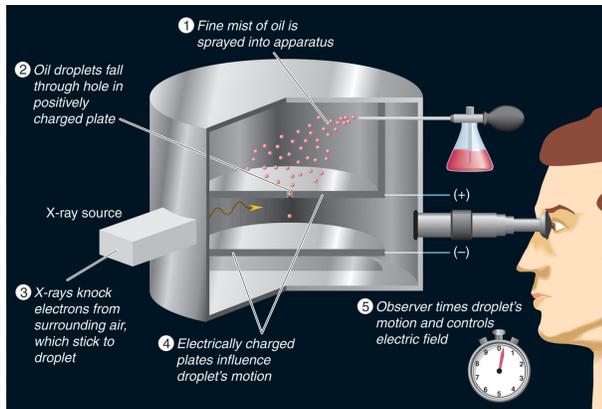
1. All matter consists of **atoms**.
2. All atoms of a given element are identical, having the same size, mass and chemical properties.
3. The atoms of one element are different from the atoms of all other elements.
4. Chemical reactions only involve the rearrangement of atoms. Atoms are not created or destroyed in chemical reactions.

J.J. Thomson (1906 Nobel Prize in Physics)



→ measured mass/charge of e^-

Millikan's Oil-Drop Experiment for Measuring an Electron's Charge



Millikan

1923 Nobel Prize in Physics

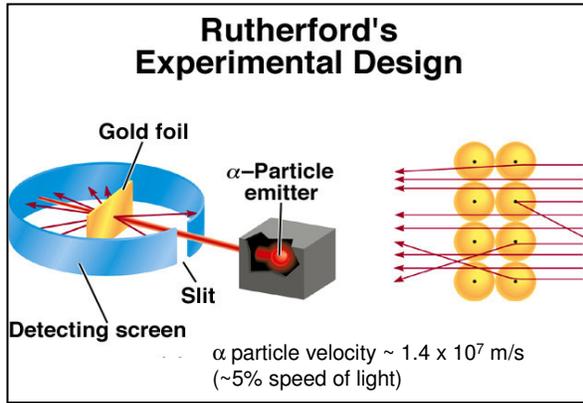
Measured mass of e^-

$$e^- \text{ charge} = -1.60 \times 10^{-19} \text{ C}$$

$$\text{Thomson's charge/mass of } e^- = -1.76 \times 10^8 \text{ C/g}$$

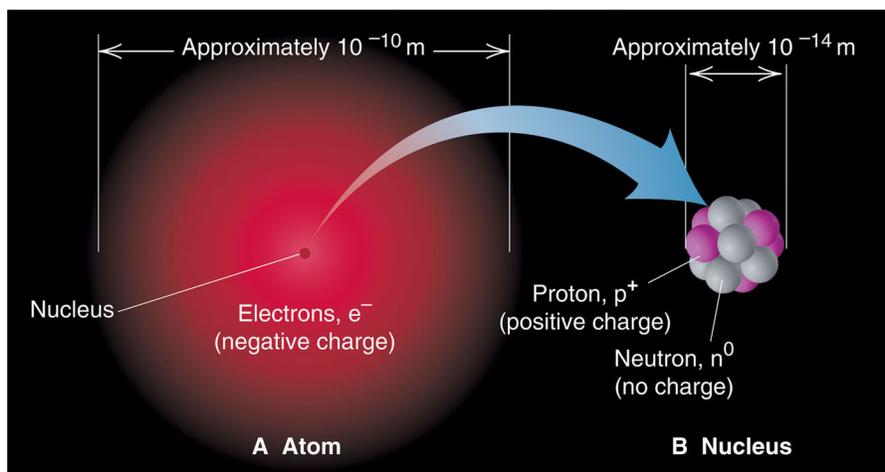
$$e^- \text{ mass} = 9.10 \times 10^{-28} \text{ g}$$

Rutherford (1908 Nobel Prize in Chemistry)



1. atoms positive charge is concentrated in the nucleus
2. proton (p) has opposite (+) charge of electron (-)
3. mass of p is 1840 x mass of e^- (1.67×10^{-24} g)

Model of the Atom



Substances - Definitions

Element: Substance built from atoms with the same proton number
Number of neutrons can vary

Isotopes of Carbon

Element: C ^{12}C , ^{13}C



Substance built from atoms with the same proton number and a defined number of neutrons: **Nuclide**

Compound: Substance built from atoms with different proton numbers.

Element - Symbols

Characterisation of atoms/elements/compounds

Symbols consist of one to three letters; usually derived from the latin name of the element

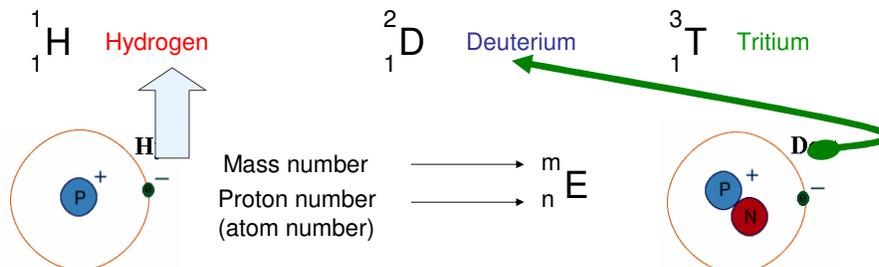
H: Hydrogen (hydrogenium)

N: Nitrogen (nitrogenium)

C: Carbon (carbenium)

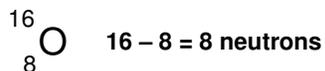
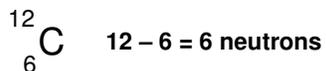
O: Oxygen (oxygenium)

Isotopes have usually the same symbol. Exception: Hydrogen



Element - Symbols

Information from the symbols



Isotope nomenclature: ${}^{12}_6\text{C}$

Called: Carbon-12 or C-12

Isotope abundance:



Generally the percentage contributions of heavier isotopes increases for the heavier elements

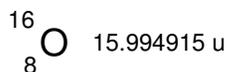
Masses of Atoms and Elementary Particles

1 atom of the carbon isotope ${}^{12}_6\text{C}$ weighs 12 u or $1.99264 \cdot 10^{-26}$ kg

that means $1\text{u} = 1.66053 \cdot 10^{-27}$ kg

Neutron: 1.00866 u; proton: 1.00727 u; electron $5.48593 \cdot 10^{-4}$ u

Masses of nuclides:



Atomic and molecular mass

average atomic mass:

$$M_{\text{Atom}} = \frac{\Sigma(\text{nuclide mass} \cdot \text{abundance})}{100}$$

Example: Cl

$$\bar{M}(\text{Cl}) = \frac{(34.9689 \cdot 75.53) + (36.9659 \cdot 24.47)}{100}$$
$$\bar{M}(\text{Cl}) = 35.453 \text{ u}$$

average molecular mass: $\bar{M}_{\text{molecule}}$

Example Cl₂ gas:

$$\bar{M}(\text{Cl}_2) = 35.453\text{u} \cdot 2 = 70.906 \text{ u}$$

Using relative atomic masses to count atoms – the mole

Counting unit on an atomic scale: The Mole n (symbol: mol; SI unit)

1 Mole of a substance contains as many particles (atoms, molecules, etc) as there are atoms in exactly 12 g of the nuclide 12-carbon (¹²C).

The number N_A of particles in 1 Mole is $6.022 \cdot 10^{23}$!!!!

1 mol Al contains $6.022 \cdot 10^{23}$ Al atoms.
1 mol H₂O contains $6.022 \cdot 10^{23}$ H₂O molecules.

Mass of 1 Mole of C → molar mass of C = $M(\text{C}) = 12\text{g/mol}$

Mass of 1 Mole of H₂O → molar mass of H₂O =
 $M(\text{H}_2\text{O}) = 18.015\text{u} \times 6.022 \cdot 10^{23} = 18.015 \text{ g/mol}$

Formula to learn by heart !!!!:

$$\text{number of moles} = \frac{\text{grams of substance}}{\text{molar mass}}$$

$$n = \frac{m}{M} \left[\frac{\text{g}}{\text{g/mol}} = \text{mol} \right]$$